

Crystal Structure of Thorium Nitrate Pentahydrate by X-ray Diffraction*

BY TATZUO UEKI, ALLAN ZALKIN AND DAVID H. TEMPLETON

Lawrence Radiation Laboratory and Department of Chemistry, University of California, Berkeley, California 94720, U.S.A.

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Crystals of $\text{Th}(\text{NO}_3)_4 \cdot 5\text{H}_2\text{O}$ are orthorhombic, space group $Fdd2$, $a=11.182$, $b=22.873$, $c=10.573$ Å, $Z=8$. Thorium has three water molecules and eight oxygen atoms from four nitrate ions as neighbors in a highly polar arrangement. All hydrogen atoms are in hydrogen bonds 2.71 to 2.96 Å in length. Average bond distances are: Th–O (water) 2.46 Å, Th–O (nitrate) 2.57 Å, N–O (next to Th) 1.27 Å, N–O (terminal) 1.22 Å. An error of about 0.05 Å is made in the position of the thorium atom if anomalous dispersion ($\Delta f''=9$) is neglected.

Thorium nitrate crystallizes readily from aqueous nitric acid solutions as the pentahydrate, $\text{Th}(\text{NO}_3)_4 \cdot 5\text{H}_2\text{O}$. The earlier literature is confused and contradictory concerning its composition, and it is often found in chemical store rooms labeled as $\text{Th}(\text{NO}_3)_4 \cdot 4\text{H}_2\text{O}$. Ferraro, Katzin & Gibson (1954) made a definitive study of the phase diagram and showed that the tetrahydrate crystallizes only when the nitric acid concentration is very high.

An earlier X-ray study of the pentahydrate, then referred to as the hexahydrate, revealed the unit cell, space group, and thorium atom positions (Templeton & Dauben, 1950). No attempt was made at that time to determine the rest of the structure. With the advantage of electronic computers and better methods for X-ray intensity measurement, we recently solved the structure as reported in the present paper. An independent analysis by neutron diffraction, with results in good agreement with ours, is described in the adjacent paper (Taylor, Mueller & Hitterman, 1966). These studies confirm the composition, show an interesting coordination geometry for the thorium ions, and reveal an intricate structure of hydrogen bonds.

Experimental

A bottle from Allied Chemical, General Chemical Division, New York, and labeled $\text{Th}(\text{NO}_3)_4 \cdot 4\text{H}_2\text{O}$ contained large clear colorless crystals and white powder. Our X-ray diffraction data were obtained from a fragment with dimensions $0.22 \times 0.08 \times 0.08$ mm which was cut from one of the clear crystals. It was sealed in a silica-glass capillary (wall thickness 0.01 mm) to prevent deliquescence. Cell dimensions and intensities were measured with the General Electric XRD-5 goniostat with scintillation counter and pulse-height discriminator, using molybdenum radiation. Cell dimensions are based on $\lambda(K\alpha_1)=0.70926$ Å. Intensities of 1036 independent reflections (121 recorded as zero) were meas-

ured with the stationary-crystal technique and a counting time of 10 sec. A search for violations of the rules of space group $Fdd2$ failed to detect any. The thorium atoms in the special positions $8(a)$ cause intensities to be weak if $h+k+l=4n+2$, especially at large diffraction angles. For fear that many weak or zero data would be undesirable in the least-squares calculations, we assigned zero weight to the 156 reflections with 2θ greater than 40° and with counting rates of 2 counts/sec or less. No correction was made for absorption or extinction. We estimate the absorption parameter μR as 1.3 for the smaller dimensions of the crystal, and this effect is the dominant source of error in the thermal parameters.

Calculations were made with an IBM 7044 computer using an unpublished full-matrix least-squares program which minimizes $\sum w(|F_o|-|F_c|)^2/\sum w|F_o|^2$. The weights w were taken as unity or zero. Atomic scattering factors for Th^{4+} were obtained by extrapolation from the values for Yb^{4+} and Hg^{4+} (Thomas & Umeda, 1957) with corrections $\Delta f'=-6$ and $\Delta f''=9$ for anomalous dispersion. For nitrogen and oxygen we used form factors for neutral atoms as listed by Ibers (1962).

Unit cell and space group

$\text{Th}(\text{NO}_3)_4 \cdot 5\text{H}_2\text{O}$ crystals are orthorhombic, space group $Fdd2$, with 8 formula units in the cell:

$$\begin{aligned} a &= 11.182 \pm 0.003 \text{ \AA} \quad (11.191 \pm 0.007 \text{ \AA}), \\ b &= 22.873 \pm 0.005 \quad (22.889 \pm 0.015 \text{ \AA}), \\ c &= 10.573 \pm 0.003 \quad (10.579 \pm 0.007 \text{ \AA}). \end{aligned}$$

The dimensions found by Taylor, Mueller & Hitterman (1966) are given in parentheses. The discrepancy of 6 to 8 parts in 10,000 is only slightly more than one

Table 1. Approximate hydrogen coordinates

Atom	x	y	z
H(1)	0.05	0.04	0.25
H(2)	0.17	0.14	0.34
H(3)	0.31	0.13	0.31
H(4)	-0.05	0.11	0.41
H(5)	0.10	0.07	0.49

* Work done under the auspices of the U.S. Atomic Energy Commission.

Table 2. Structure factor magnitudes, observed (FOB) and calculated (FCA)

An asterisk indicates zero weight.

H,K= 0, 0	H,K= 0,30	7 134 142	12 185 179	0 193 190	5 224 229	L FOB FCA	8 173 163	3 254 244
L FOB FCA	L FOB FCA	9 153 156	14 0 3*	2 0 28*	7 188 182	0 116 112		5 217 207
4 660 668	2 175 178	11 110 109		4 206 198	9 169 156	2 398 423	H,K= 4,26	7 161 154
8 263 256			H,K= 2, 8	6 0 17*	11 109 116,	4 107 107	L FOB FCA	9 152 144
12 191 193	H,K= 0,32	H,K= 1,19	L FOB FCA	8 156 144		6 397 412	0 0 12*	11 106 100
	L FOB FCA	L FOB FCA	0 125 121		H,K= 3,17	8 71 57	2 213 200	
H,K= 0, 2	L FOB FCA	L FOB FCA	2 576 572	H,K= 2,28	L FOB FCA	10 215 215	4 0 15*	H,K= 5,17
L FOB FCA	L FOB FCA	L FOB FCA	4 67 63	L FOB FCA	L FOB FCA	12 0 4*	6 174 174	L FOB FCA
10 241 249	H,K= 1, 1	5 184 181	6 360 373	0 0 3*	3 273 265	14 117 112		1 214 216
14 134 124	L FOB FCA	7 161 176	8 46 52	2 168 164	5 228 221		H,K= 4,28	3 193 200
	L FOB FCA	1 471 461	10 234 233	4 0 4*	7 179 182		L FOB FCA	5 159 159
	H,K= 0, 4	3 352 351	11 101 99	12 0 2*	6 146 141	9 165 164	L FOB FCA	7 120 130
L FOB FCA	5 427 441		14 127 122			11 86 95	0 533 549	2 35 25*
0 699 712	7 242 252	H,K= 1,21		L FOB FCA	H,K= 2,30	2 90 84	4 196 183	11 81 92
4 661 669	9 201 207	L FOB FCA	H,K= 2,10	L FOB FCA	H,K= 3,19	4 390 402	6 0 13*	
8 318 331	11 135 139	L FOB FCA	L FOB FCA	0 182 175	L FOB FCA	6 42 50		H,K= 5,19
12 167 167	13 117 120	3 216 206	0 719 705	2 0 25*	L FOB FCA	8 254 259	L FOB FCA	1 228 231
		5 200 200	2 65 63	4 147 146	3 249 238	10 31 31*	L FOB FCA	3 183 176
H,K= 0, 6	H,K= 1, 3	7 135 135	4 389 393		5 191 199	12 148 157	0 0 25*	5 163 168
L FOB FCA	L FOB FCA	9 124 116	6 34 33	H,K= 3, 1	7 136 132		2 179 170	7 125 138
2 800 836	L FOB FCA	11 98 92	8 300 300	L FOB FCA	9 111 116	H,K= 4,10		9 109 117
6 374 391	3 340 356		10 0 17*	1 418 424	11 81 90	L FOB FCA	H,K= 5, 1	11 74 88
10 198 206	5 339 343	H,K= 1,23	12 200 183	3 442 443		L FOB FCA	L FOB FCA	
14 130 128	7 227 234	L FOB FCA	14 0 7*	5 351 348	H,K= 3,21	2 405 400	H,K= 5, 1	
	9 234 233	L FOB FCA		7 162 161	L FOB FCA	4 33 37	L FOB FCA	H,K= 5,21
H,K= 0, 8	11 174 171	3 186 185	H,K= 2,12	9 182 179	1 199 188	6 322 319	5 268 271	L FOB FCA
L FOB FCA	15 102 111	5 141 145	L FOB FCA	11 127 121	3 167 181	8 0 30	7 209 207	1 219 225
0 522 510		7 133 136	0 20 26	13 109 102	5 159 153	10 179 177	9 193 190	3 204 211
4 504 523	H,K= 1, 5	9 113 110	2 438 421		7 134 131	12 0 4*	11 131 138	5 155 159
8 260 263	L FOB FCA		4 79 73	H,K= 3, 3	9 104 111		13 100 106	7 121 117
12 140 146	1 415 403	H,K= 1,25	6 313 304	L FOB FCA		H,K= 4,12		9 101 112
	3 353 341	L FOB FCA	8 40 28	1 347 347	H,K= 3,23	L FOB FCA	H,K= 5, 3	
H,K= 0,10	5 346 355	1 171 162	10 245 239	3 336 341	L FOB FCA	0 458 463	L FOB FCA	H,K= 5,23
L FOB FCA	7 307 314	3 149 141	12 34 4*	5 326 333	1 159 162	2 32 28	L FOB FCA	L FOB FCA
2 586 581	9 198 201	5 159 159		7 245 252	3 171 166	4 347 352	3 414 411	1 153 149
6 317 327	11 159 155	7 135 125	H,K= 2,14	9 187 181	5 167 174	6 46 41	5 325 318	3 146 144
10 178 176	13 103 100	9 111 106	L FOB FCA	11 102 104	7 140 139	8 253 243	7 223 225	5 141 145
14 98 103			0 455 454	13 98 91	9 95 97	10 0 20*	9 218 210	7 110 122
			2 60 47			12 132 135	11 157 153	9 117 114
H,K= 0,12	H,K= 1, 7	H,K= 1,27	4 412 417	H,K= 3, 5	H,K= 3,25		13 100 104	
L FOB FCA	L FOB FCA	L FOB FCA	6 46 24	L FOB FCA	L FOB FCA	H,K= 4,14		H,K= 5,25
0 539 535	3 435 436	3 164 167	8 300 300	1 412 421	1 135 132	L FOB FCA	H,K= 5, 5	L FOB FCA
4 415 416	5 199 213	5 115 110	10 0 21*	3 310 316	3 134 135	0 115 120	L FOB FCA	1 174 172
8 280 274	7 271 280	7 89 104		5 310 313	5 143 138	2 285 289	1 403 407	3 142 138
12 128 122	9 220 225			7 267 270	7 100 110	4 72 57	3 301 316	5 138 134
	11 139 140	H,K= 1,29	H,K= 2,16	9 203 200		6 283 279	5 246 243	7 120 117
L FOB FCA	L FOB FCA	L FOB FCA	L FOB FCA	11 156 147	H,K= 3,27	8 0 14*	7 201 205	
2 309 309	H,K= 1, 9	3 106 109	2 314 312	13 98 98	L FOB FCA	10 171 181	9 186 184	H,K= 5,27
6 283 274	L FOB FCA	5 103 117	4 51 46		1 130 133	12 0 12*	11 125 124	L FOB FCA
10 165 169	1 344 334		6 309 317	H,K= 3, 7	3 113 111		13 94 102	1 158 157
	3 415 408	H,K= 1,31	8 43 44*	L FOB FCA	5 117 109	H,K= 4,16		3 140 138
H,K= 0,16	5 274 278	L FOB FCA	10 201 205	3 395 402	7 90 96	L FOB FCA	H,K= 5, 7	5 120 133
L FOB FCA	7 214 218	1 103 114	12 0 7*	5 268 266		0 315 305	L FOB FCA	
0 447 430	9 193 190	3 111 111		9 207 207	H,K= 3,29	2 26 9	L FOB FCA	H,K= 5,29
4 386 387	11 126 126		H,K= 2,18	7 166 167	L FOB FCA	4 337 330	3 232 227	L FOB FCA
8 182 193	13 99 106	H,K= 2, 0	L FOB FCA	14 138 137	1 153 153	6 57 66	5 308 304	1 108 108
12 113 117		L FOB FCA	0 360 353	13 93 98	3 113 114	8 217 209	7 256 256	3 116 107
	H,K= 1,11	2 281 274	2 37 22		5 97 112	10 0 6*	9 179 172	
H,K= 0,18	L FOB FCA	6 373 375	4 327 325	H,K= 3, 9	H,K= 3,31	12 110 116	11 108 112	H,K= 6, 0
L FOB FCA	L FOB FCA	10 263 248	6 0 13*	L FOB FCA	L FOB FCA		13 72 87	L FOB FCA
2 355 343	3 371 375	14 119 116	8 196 197	1 517 510	1 104 104	H,K= 4,18		2 500 501
6 265 285	5 256 267		10 0 3*	3 322 326		0 38 26	L FOB FCA	6 285 283
10 159 147	7 196 196	H,K= 2, 2	12 133 130	5 275 279	H,K= 4, 0	2 345 340	L FOB FCA	10 201 201
	9 156 163	L FOB FCA		7 219 212	L FOB FCA	4 28 21	3 282 288	H,K= 6, 2
H,K= 0,20	11 107 110	0 604 593	H,K= 2,20	9 147 147	0 683 702	6 216 213	5 303 298	L FOB FCA
L FOB FCA	13 101 103	2 91 88	L FOB FCA	11 101 114	4 533 536	8 46 22*	7 180 177	0 448 456
0 418 424		4 480 492	0 38 30	13 87 107	8 337 321	10 144 148	9 147 149	2 42 43
4 261 259	H,K= 1,13	6 30 34	2 303 293		12 155 159		11 133 124	4 383 386
8 171 160	L FOB FCA	8 517 318	4 41 41	H,K= 3,11		H,K= 4,20	13 89 87	6 79 72
	1 260 264	10 0 22	6 250 246	L FOB FCA	H,K= 4, 2	L FOB FCA		8 295 286
H,K= 0,22	3 210 211	12 168 168	8 0 22*	1 400 400	L FOB FCA	0 321 309	H,K= 5,11	10 31 35*
L FOB FCA	5 314 317	14 0 11*	10 149 152	3 358 352	0 127 118	2 64 63	L FOB FCA	12 161 163
2 317 327	7 176 179			5 301 307	2 540 558	4 260 263	1 317 315	
6 202 196	9 191 188	H,K= 2, 4	H,K= 2,22	7 211 213	4 144 133	6 31 21*	3 212 216	H,K= 6, 4
10 145 143	11 114 121	L FOB FCA	L FOB FCA	9 175 177	6 340 339	8 174 174	5 214 218	L FOB FCA
	13 73 91	0 165 147	0 227 229	11 131 134	8 64 62	10 0 17*	7 140 144	0 0 1
		2 361 387	2 29 11*	13 63 98	10 252 240	9 119 115	9 119 115	2 335 333
H,K= 0,24	L FOB FCA	4 109 115	4 226 225		12 0 11*	11 101 107	11 101 107	4 73 65
0 275 271	L FOB FCA	6 410 414	6 55 34	H,K= 3,13	L FOB FCA	13 83 89	13 83 89	6 345 354
4 240 246	1 264 255	8 0 25	8 201 200	L FOB FCA	0 30 36*			8 0 29
8 192 195	3 189 189	10 246 246	10 0 2*	1 365 355	H,K= 4, 4	2 274 258	H,K= 5,13	10 232 228
	5 281 273	12 0 20*		3 313 313	L FOB FCA	4 44 37*	L FOB FCA	12 0 6*
H,K= 0,26	7 217 222	14 125 130	H,K= 2,24	5 289 277	0 460 480	6 196 193	L FOB FCA	
L FOB FCA	9 160 152		L FOB FCA	7 161 161	2 60 50	8 0 10*	3 204 205	H,K= 6, 6
2 228 240	11 117 119	H,K= 2, 6	0 31 4*	4 94 162	4 494 504	10 134 133	5 241 235	L FOB FCA
6 151 165	13 74 82	L FOB FCA	2 205 191	11 125 120	6 52 56		7 224 216	0 445 445
		0 240 243	4 0 21*	13 90 92	8 322 317	H,K= 4,24	9 161 152	2 110 107
H,K= 0,28	H,K= 1,17	4 488 497	6 176 178	H,K= 3,15	10 0 20*	L FOB FCA	11 60 86	4 389 384
L FOB FCA	L FOB FCA	6 45 45	8 0 15*	L FOB FCA	12 166 162	0 268 258		6 118 105
0 213 233	1 288 285			L FOB FCA	14 0 9*	2 0 15*	H,K= 5,15	8 278 269
4 215 215	3 211 200	8 344 343	H,K= 2,26	1 332 327	4 221 216	6 0 14*	L FOB FCA	10 0 17*
	5 216 209	10 0 19*	L FOB FCA	3 209 208			1 213 207	12 156 155

Table 2 (cont.)

H,K=6, 8	C 0 33*	9 72 93	H,K=8,14	3 186 185	6 31 21*	7 125 115	H,K=12, 8	5 104 110
L FOB FCA	2 166 168		L FOB FCA	5 211 209	8 213 215	9 112 105	L FOB FCA	
0 94 98	4 0 21*	H,K=7,21	0 40 38	7 134 128	10 0 5*		L FOB FCA	H,K=13,15
2 365 362		L FOB FCA	2 333 331	9 144 137			2 32 22*	L FOB FCA
4 42 43	H,K=7, 1	1 173 159	4 0 7*	11 110 105	H,K=10, 8	H,K=11, 7	4 224 216	1 119 123
6 296 290	L FOB FCA	3 116 110	6 246 244		L FOB FCA	L FOB FCA	6 0 9*	3 96 105
8 29 48*	1 277 291	5 160 154	8 0 13*		0 40 19	3 165 158	8 145 152	
10 208 201	3 251 246	7 116 113	10 143 142	H,K=9,11	L FOB FCA	5 219 214		H,K=13,17
12 0 8*	5 256 245	9 98 97		1 182 176	2 231 223	4 30 24*	H,K=12,10	L FOB FCA
	7 217 200			3 173 165	6 229 228	9 102 97	L FOB FCA	1 97 108
	9 142 136	H,K=7,23	H,K=8,16	5 160 158	8 0 17*		0 32 9*	3 112 112
H,K=6,10	11 121 118	L FOB FCA	0 311 311	7 158 156	10 149 152	H,K=11, 9	2 231 225	
L FOB FCA	13 82 83	L FOB FCA	2 0 15*	9 124 127		L FOB FCA	4 0 3*	H,K=14, 0
0 396 388		1 144 147	4 243 231	11 91 94	H,K=10,10	1 224 218	6 185 192	L FOB FCA
2 41 36	H,K=7, 3	3 134 141	6 46 27*		L FOB FCA	3 179 176	8 0 10*	2 201 209
4 379 373	L FOB FCA	5 125 126	8 191 185	H,K=9,13	0 264 259	5 162 162	6 172 183	
6 0 15	1 264 266	7 109 107	10 0 10*	L FOB FCA	2 0 14*	7 123 121		
8 251 244	3 205 210	H,K=7,25	H,K=8,18	1 190 185	4 264 264	9 89 95	H,K=12,12	L FOB FCA
10 0 13*	5 205 209	L FOB FCA	3 163 153	3 163 153	6 0 17*	0 229 222	L FOB FCA	H,K=14, 2
12 129 133	7 211 214	1 97 103	L FOB FCA	5 139 130	8 160 160	2 0 13*	0 209 226	L FOB FCA
	9 146 136	3 105 119	0 0 2*	7 136 138	10 0 3*	4 191 200	2 35 2*	0 209 226
H,K=6,12	11 106 96	5 120 123	2 263 264	9 111 120		1 235 229	6 0 9*	4 187 191
L FOB FCA	13 82 88		4 45 10*		H,K=10,12	3 177 167	6 0 12*	6 0 12*
0 81 79		H,K=7,27	6 185 185	H,K=9,15	L FOB FCA	5 155 149	H,K=12,14	
2 328 313	H,K=7, 5	L FOB FCA	8 0 13*	L FOB FCA	0 67 71	7 98 110	L FOB FCA	H,K=14, 4
4 37 44	L FOB FCA	1 102 114		1 124 125	2 229 223	9 90 87	0 34 1*	L FOB FCA
6 282 284	1 187 183	3 97 100	H,K=8,20	3 202 200	4 0 30*		2 205 213	0 34 23*
8 0 25*	3 294 284		L FOB FCA	5 147 139	6 227 224	H,K=11,13	4 0 10*	2 181 190
10 189 183	5 284 275	H,K=9, 0	0 270 268	7 151 145	8 0 24*	L FOB FCA	6 178 174	4 50 21*
12 0 7*	7 190 19C	L FOB FCA	2 0 16*	9 108 115	10 123 127	1 172 166		6 156 160
	9 200 186	4 374 381	4 226 231			3 146 160	H,K=12,16	
H,K=6,14	11 117 104	4 370 370	6 0 4*	H,K=9,17	H,K=10,14	5 162 153	L FOB FCA	H,K=14, 6
L FOB FCA	13 83 89	8 210 207	8 136 135	L FOB FCA	L FOB FCA	7 128 139	0 194 190	L FOB FCA
0 304 299		12 119 125		1 155 152	0 177 174		2 0 7*	0 184 190
2 90 82	H,K=7, 7		H,K=8,22	3 127 127	2 31 11*	H,K=11,15	4 168 177	2 0 7*
4 306 304	L FOB FCA	H,K=8, 2	L FOB FCA	5 169 155	4 206 203	L FOB FCA	6 0 20*	4 172 180
6 29 24*	1 292 292	L FOB FCA	0 47 23*	7 130 124	0 0 19*	1 161 157		6 0 7*
8 229 231	3 263 264	0 53 40	2 171 170	9 83 91	8 171 169	3 174 171	H,K=12,18	H,K=14, 8
10 0 6*	5 259 254	4 414 417	4 0 15*			5 143 138	L FOB FCA	L FOB FCA
12 128 134	7 166 162	4 0 5	6 164 173	H,K=9,19	H,K=10,16	7 115 109	0 36 14*	L FOB FCA
	9 165 155	6 313 301		L FOB FCA	L FOB FCA		2 173 177	0 35 15*
H,K=6,16	11 119 120	8 0 33*	H,K=8,24	1 79 160	0 32 5*	H,K=11,17	4 0 7*	2 170 187
L FOB FCA		10 147 140	L FOB FCA	3 74 144	2 214 215	L FOB FCA	4 0 9*	4 0 9*
0 60 59	H,K=7, 9	12 0 4*	0 169 182	5 70 117	4 0 29*	1 155 161	H,K=12,20	H,K=14,10
2 288 285	L FOB FCA		2 0 0*	7 62 108	6 176 170	3 158 160	L FOB FCA	L FOB FCA
4 28 46	1 334 328	H,K=8, 4	4 178 177		3 0 9*	5 123 122	0 173 169	0 178 173
6 260 253	3 242 226	L FOB FCA	6 0 15*	H,K=9,21	H,K=10,18	7 105 100	2 0 9*	2 0 6*
8 0 21*	5 231 229	0 469 466		L FOB FCA	L FOB FCA			4 151 161
10 164 158	7 140 148	2 49 51	H,K=8,26	1 151 151	L FOB FCA	H,K=11,19	H,K=13, 1	
	9 159 153	4 354 340	L FOB FCA	3 128 120	0 204 221	L FOB FCA	L FOB FCA	L FOB FCA
H,K=6,18	11 115 110	6 0 20	0 0 17*	5 137 140	2 0 14*	1 131 145	1 163 160	H,K=14,12
L FOB FCA		8 219 215	2 154 163	7 104 98	4 187 190	3 147 152	3 169 161	L FOB FCA
0 296 294	H,K=7,11	10 0 2*	4 0 5*		6 0 21*	5 103 118	5 119 124	0 0 2*
2 41 25	L FOB FCA	12 120 127		H,K=9,23	H,K=10,20		7 119 116	2 164 166
4 269 258	1 297 298		H,K=9, 1	L FOB FCA	L FOB FCA	H,K=11,21		4 0 4*
6 31 17*	3 273 271	H,K=8, 6	L FOB FCA	1 121 126	0 0 8*	1 135 143	H,K=13, 3	H,K=14,14
8 198 195	5 213 210	L FOB FCA	1 277 268	3 137 114			L FOB FCA	L FOB FCA
10 0 6*	7 181 186	0 43 37	3 241 230	5 110 105	2 189 190	3 116 120	1 150 145	L FOB FCA
	9 145 151	2 343 343	5 181 190		4 35 6*		3 124 134	0 139 143
H,K=6,20	11 112 112	4 53 40	7 208 194	H,K=9,25	6 137 136	H,K=11,23	5 158 155	2 0 13*
L FOB FCA		6 271 263	9 142 143	L FOB FCA		L FOB FCA	7 125 122	
0 0 22*	H,K=7,13	8 31 8*	11 118 114	1 107 111		1 124 116		H,K=15, 1
2 259 250	L FOB FCA	10 186 179		3 93 102	H,K=10,22	L FOB FCA	H,K=13, 5	L FOB FCA
4 31 49*	1 276 264	12 0 5*	H,K=9, 3		L FOB FCA	0 191 198	1 136 142	1 140 149
6 190 187	5 249 250		L FOB FCA	H,K=10, 0	2 0 27*	L FOB FCA	3 138 147	3 110 111
8 0 8*	5 204 200	H,K=8, 8	1 252 237	L FOB FCA	4 167 176	0 176 177	5 143 141	H,K=15, 3
10 139 140	7 162 159	L FOB FCA	3 235 222	2 392 401		4 230 226	8 142 146	L FOB FCA
	9 152 148	0 472 473	5 221 213	6 230 232	H,K=10,24	0 0 5*		1 135 129
H,K=6,22	11 106 106	2 51 42	9 154 152	10 169 164	L FOB FCA			3 104 121
L FOB FCA		4 381 378	9 154 152		0 0 5*	H,K=12, 2	H,K=13, 7	
0 243 254	H,K=7,15	6 41 42*	11 133 122	H,K=10, 2	2 143 150	L FOB FCA	L FOB FCA	H,K=15, 5
2 45 61*	L FOB FCA	8 214 201		L FOB FCA		0 31 11*	1 149 151	L FOB FCA
4 211 218	1 192 198	10 34 10*	H,K=9, 5	0 300 301	H,K=11, 1	2 237 232	3 152 142	L FOB FCA
6 34 16*	3 225 224	12 122 113	L FOB FCA	2 39 57	L FOB FCA	4 32 17*	5 131 142	1 115 119
6 156 154	5 171 168		1 152 145	4 300 289	1 256 250	6 193 187	7 104 104	3 98 113
	7 185 184	H,K=8,10	3 217 214	0 0 11*	3 236 229	8 0 9*		
H,K=6,24	9 140 138	L FOB FCA	5 253 247	8 224 218	5 139 140		H,K=13, 9	H,K=15, 7
L FOB FCA	11 82 88	0 26 10	7 178 173	10 0 12*	7 144 133	H,K=12, 4	L FOB FCA	L FOB FCA
0 0 14*		2 423 417	9 175 169		9 111 108	L FOB FCA	1 159 162	1 110 115
2 169 172	H,K=7,17	4 39 25	11 108 99	H,K=10, 4		0 219 217	3 138 146	3 118 119
4 0 5*	L FOB FCA	6 200 204		L FOB FCA	H,K=11, 3	2 31 9*	5 118 110	
6 173 178	1 223 227	8 0 2*	H,K=9, 7	0 39 14	L FOB FCA	4 223 211	7 98 105	H,K=15, 9
8 0 7*	3 193 183	10 165 162	L FOB FCA	2 280 273	1 212 217	6 34 13*		L FOB FCA
	5 209 204		1 221 223	4 29 33*	3 209 198	8 182 180	H,K=13,11	1 98 106
H,K=6,26	7 150 155	H,K=8,12	3 182 175	0 255 249	5 162 161		L FOB FCA	
L FOB FCA	9 111 110	L FOB FCA	5 200 200	8 0 12*	7 140 132	H,K=12, 6	1 150 158	
0 182 186		0 379 364	7 164 153	10 170 174	9 122 110	L FOB FCA	3 126 124	
2 35 10*	H,K=7,19	2 39 21	9 138 133			0 44 35*	5 114 119	
4 177 168	L FOB FCA	4 310 308	11 109 103	H,K=10, 6	H,K=11, 5	2 197 195		
6 0 18*	1 200 199	6 0 2*		L FOB FCA	L FOB FCA	4 0 9*		
	3 179 183	8 178 183	H,K=9, 9	0 345 347	1 208 208	6 195 186	H,K=13,13	
H,K=6,28	5 170 165	10 0 6*	L FOB FCA	2 57 53	3 215 214	8 0 12*	L FOB FCA	
L FOB FCA	7 107 124		1 217 214	4 271 268	5 169 173		3 138 128	

would expect from the estimated standard deviations. The density calculated from our data, 2.800 ± 0.002 g.cm⁻³, is between the density measured by flotation in this laboratory, 2.84, and that reported by Staritzky (1956), 2.787. Our measurements were made at about 21°C.

Crystal data for the isomorphous cerium and plutonium compounds are given by Staritzky (1956). These crystals are expected to have very nearly the same atomic arrangement.

Determination of the structure

The thorium atoms are in the special position set 8(a): (0,0,z; $\frac{1}{4}$, $\frac{1}{4}$, $\frac{1}{4}+z$)+F, and for this first atomic set z can be taken as zero. Refinement of the two parameters (scale factor and isotropic thermal parameter) reduced $R = \Sigma ||F_o| - |F_c|| / \Sigma |F_o|$ to 0.147. This partial structure has symmetry *Fddd*, and therefore a Fourier calculation phased by the thorium atom shows duplicate images of the rest of the structure. Furthermore, no phase information is obtained for reflections with $h+k+l=4n+2$, which constitute about one-fourth of the data. The structure was solved by selecting various peaks in the Fourier functions as trial atoms and testing the behavior of their thermal parameters in least-squares calculations. At the third round of this, the nitrate groups were recognized. After several more trials, *R* was reduced to 0.077 (isotropic thermal parameters) or 0.062 (thorium atom anisotropic) with one water molecule not correctly placed. The correct structure gave $R=0.043$, with only the thorium atom anisotropic. Further refinement with anisotropic thermal parameters for all atoms (hydrogen excluded) reduced *R* to 0.034.

We had proceeded with the assumption that the water content was in doubt. To check for additional water molecules, we calculated a Fourier synthesis of ($F_o - F_c$), deleting reflections with zero intensity. The largest peaks in this function were about 0.28 e.Å⁻³, in the neighborhood of the thorium atom. No evidence was found of further water molecules. With the help of an assignment of hydrogen bonds five peaks about one-third to one-half as high as the largest were selected as hydrogen atoms (Table 1). No attempt was made to include hydrogen in any of the structure factor calculations, or to refine these positions.

The calculations to this point had neglected the out-of-phase component $\Delta f''$ of thorium. Because of the polar nature of the space group *Fdd2*, two orientations of the structure must be considered, one of which is the reflection of the other in (001). Further calculations with $\Delta f''$ included and the correct orientation reduced *R* to 0.033 (or 0.045 including reflections of zero weight). With the reverse structure *R* could not be reduced below 0.035, and the weighted sum of squares was 15% larger. In the final cycle of the correct structure, no coordinate shifted more than 0.000008 and no thermal parameter more than 0.001. Observed

and calculated structure factor magnitudes are listed in Table 2. The final coordinates are given in Table 3. The anisotropic thermal parameters (Table 4) are listed

Table 3. Atomic coordinates and estimated standard deviations

All values have been multiplied by 10⁴.

Atom	x	y	z
Th	0	0	0
O(1)	0	0	2277(17)
O(2)	2458(11)	1459(4)	3156(11)
O(3)	0457(11)	0892(5)	3934(12)
N(1)	2651(10)	0046(6)	0508(12)
O(11)	2094(9)	-0381(4)	0025(15)
O(12)	1970(10)	0453(5)	0915(13)
O(13)	3733(8)	0093(5)	0538(13)
N(2)	0471(12)	0772(5)	7741(17)
O(21)	1318(9)	0551(5)	8381(12)
O(22)	-0579(9)	0631(4)	8076(12)
O(23)	0677(12)	1066(6)	6787(12)

Table 4. Anisotropic thermal parameters

T.F. = exp ($-\beta_{11}h^2 - 2\beta_{12}hk - \dots$); $4\beta_{12} = B_{12}a^*b^*$, etc. Standard deviations estimated by least squares are less than 0.05 for Th and from 0.3 to 0.8 for the other atoms. Comparison with the neutron-diffraction results indicates standard deviations to be 1.4 for B_{33} and about 0.5 for other parameters.

Atom	B_{11}	B_{22}	B_{33}	B_{12}	B_{13}	B_{23}
Th	1.2	1.4	2.1	0.0	—	—
O(1)	4.5	2.0	3.7	0.9	—	—
O(2)	2.1	2.0	4.3	0.3	0.0	0.5
O(3)	2.4	2.6	3.3	0.1	0.6	0.2
N(1)	1.5	2.0	2.9	0.5	-0.5	-0.5
O(11)	2.2	1.4	3.8	0.8	-0.6	-0.7
O(12)	2.3	2.5	3.7	0.3	-0.2	-0.5
O(13)	1.0	2.8	5.2	-0.1	-0.5	0.0
N(2)	2.1	2.0	4.4	-0.9	0.3	0.2
O(21)	1.3	2.9	3.9	0.2	-0.3	0.9
O(22)	1.7	1.7	3.8	-0.2	-0.4	0.1
O(23)	3.5	3.6	3.0	-0.2	1.1	1.5

in the units of the isotropic Debye *B* (Zalkin, Forrester & Templeton, 1964; Cruickshank, 1965).

Effect of anomalous dispersion

Inclusion of the thorium phase shift in the calculations gives enough change in some of the structure factor magnitudes to establish the polarity of the structure, but the change in *R* is hardly dramatic. However, it causes a significant change in the structure. With the origin defined by the thorium atom, all other atoms shifted about 0.05 Å in the positive *z* direction when the correction was included. A similar shift of the reverse structure causes the two structures, after refinement, to differ by about 0.10 Å. This behavior is explained by the fact that all the calculations were made with reflections with positive values of *l*. The effect of the phase (which is an *advance* of phase) is to make the thorium atom appear to be closer to the X-ray source and detector than it really is, unless the $\Delta f''$ term is included in the structure factor calculations. The symmetry of the space group gives a cancellation

of the effect on x and y coordinates, but there is a systematic biasing of the z components of interatomic vectors between thorium and the rest of the structure.

Our data include all reflections which are in a central sphere in reciprocal space and which are not related by operations of the Laue group. Such a set is commonly described as 'complete three-dimensional data,' but it is incomplete in the sense of the crystallographic point group with the negative- l reflections missing. This kind of shift will be a general feature of polar structures which are refined with such incomplete data and with neglect of the imaginary part of the dispersion correction.

The two structures of opposite polarity are not different in the sense of right and left handedness, but only with respect to their orientation in a specimen. We have not made a correlation of the polarity with respect to morphology or other physical property.

Comparison with neutron diffraction results

The neutron diffraction study by Taylor, Mueller & Hitterman (1966) gives us a chance to check the accuracy of the X-ray method in a case where the heavy atom dominates the data. The agreement of the coordinates is excellent, and it confirms that the estimated standard deviations are of the correct magnitude. Of 31 independent coordinates, 15 are within one standard deviation and none is as much as three standard deviations from the corresponding neutron result. The atomic positions in the two structures differ by 0.026 Å on the average and by 0.045 Å in the most extreme case.

The agreement is poorer before correction for the thorium phase shift. The algebraic average Δz between neutron and X-ray coordinates is 0.0057 before and 0.0006 after this correction. We estimate that it would have been reduced to zero if $\Delta f''$ had been taken as 10 rather than 9 electrons.

The neutron results show that the hydrogen locations (Table 1) are in error by from 0.2 to 0.5 Å.

Discussion of the structure

Some interatomic distances are listed in Table 5. The thorium atom has its 11 oxygen neighbors arranged in a highly unsymmetrical way with respect to the polar direction (Fig. 1). These oxygen atoms are two each from four nitrate groups and three from water molecules, with all the water on one side. This polar arrangement is probably related to the large pyroelectric effect which is observed when the crystals are dipped in liquid nitrogen. One expects about eight oxygen neighbors for thorium if the oxygen atoms are not bonded to each other. Two oxygen atoms in nitrate are closer than normal for atoms from separate molecules, and thus the coordination can be as high as 12 if the atoms are from six nitrate groups as in $\text{MgTh}(\text{NO}_3)_6 \cdot 8\text{H}_2\text{O}$ (Ščavničar & Prodić, 1965). Thus to have eleven neighbors is reasonable if eight of them are from nitrate ions.

In each nitrate ion the non-coordinated oxygen atom is closer to nitrogen than are the other two. A similar effect is observed in several other nitrate crystals as listed by Taylor, Mueller & Hitterman (1966), as well

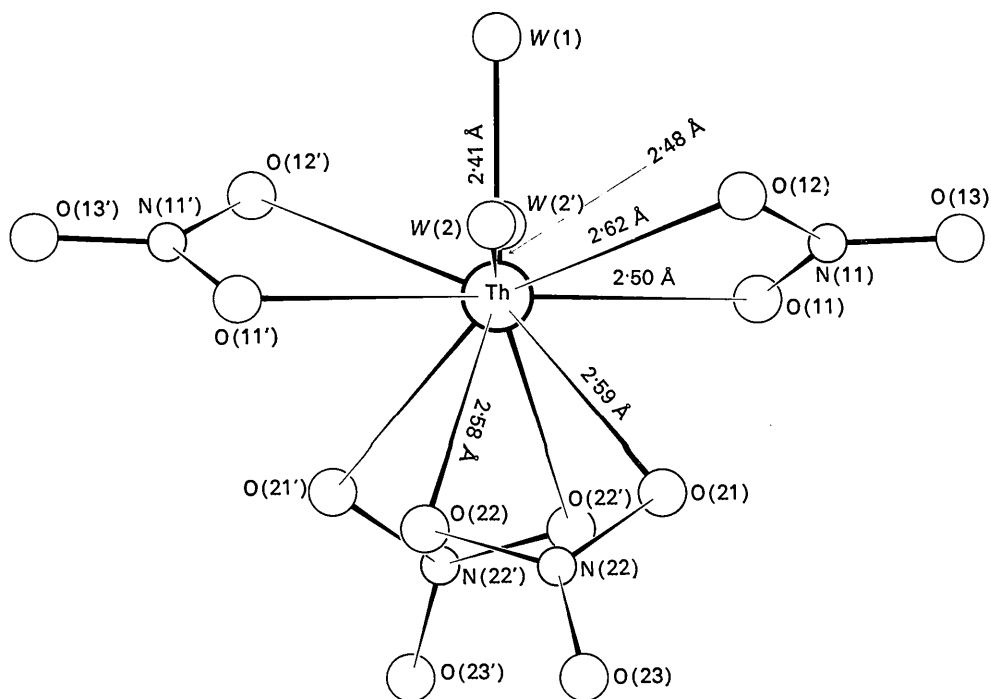


Fig. 1. Neighbors of the thorium atom in $\text{Th}(\text{NO}_3)_5 \cdot 5\text{H}_2\text{O}$, viewed down $[010]$, with $[001]$ vertical. $W(1)$ and $W(2)$ indicate water molecules called $O(1)$ and $O(2)$ in the text.

Table 5. Bond lengths (Å),
uncorrected for thermal motion

Values found by Taylor, Mueller & Hitterman are given in parentheses.

Th-O (nitrate)		
Th-O(11)	2.50 ± 0.01	(2.528)
Th-O(12)	2.62 ± 0.01	(2.618)
Th-O(21)	2.59 ± 0.01	(2.573)
Th-O(22)	2.58 ± 0.01	(2.554)
Th-O (water)		
Th-O(1)	2.41 ± 0.02	(2.438)
Th-O(2)	2.48 ± 0.01	(2.473)
Nitrate groups		
N(1)-O(11)	1.27 ± 0.02	(1.270)
N(1)-O(12)	1.28 ± 0.02	(1.250)
N(1)-O(13)	1.21 ± 0.01	(1.202)
N(2)-O(21)	1.27 ± 0.02	(1.264)
N(2)-O(22)	1.27 ± 0.02	(1.275)
N(2)-O(23)	1.24 ± 0.02	(1.206)
Hydrogen bonds		
O(1)-O(3)	2.74 ± 0.02	(2.698)
O(2)-O(3)	2.71 ± 0.02	(2.697)
O(2)-O(22)	2.90 ± 0.02	(2.953)
O(3)-O(23)	2.86 ± 0.02	(2.901)
O(3)-O(13)	2.96 ± 0.02	(2.946)

as in $\text{Ce}(\text{NO}_3)_3 \cdot 6\text{H}_2\text{O}$ and $\text{Ce}(\text{NH}_4)_2(\text{NO}_3)_6$ (Ueki, Zalkin & Templeton, unpublished). The terminal oxygen atom, in each case which we have studied, has higher thermal parameters than the other two. Thus a correction of bond distance for thermal motion removes some of the difference, but this correction seems to be inadequate to explain as much as half of the effect. In the present case, the thermal effect is estimated to account for about 0.01 Å of the difference.

We recognize five hydrogen bonds (Table 5) which are completely confirmed by the neutron diffraction results. Their distances and angles (Table 6) are normal. The hydrogen bonds to O(1), because of the twofold axis, are exactly coplanar with the Th-O(1) bond and at equal angles to it. The hydrogen bonds to O(2) are very nearly coplanar with the Th-O(2) bond. This ar-

Table 6. Bond angles

Th—O(1)—O(3)	129.8 ± 0.4°
O(3)—O(1)—O(3)	100.4 ± 0.8*
Th—O(2)—O(3)	124.0 ± 0.5
Th—O(2)—O(22)	127.2 ± 0.5
O(3)—O(2)—O(22)	108.7 ± 0.5*
O(1)—O(3)—O(2)	108.4 ± 0.5
O(1)—O(3)—O(13)	81.7 ± 0.5
O(1)—O(3)—O(23)	103.9 ± 0.5
O(2)—O(3)—O(13)	106.5 ± 0.5
O(2)—O(3)—O(23)	124.6 ± 0.6
O(13)—O(3)—O(23)	121.9 ± 0.5*

* O...H—O—H...O angles.

angement, with the water dipoles pointed almost directly away from the cation, is not surprising for such a highly charged ion. The water molecules in $\text{Zr}(\text{SO}_4)_2 \cdot 4\text{H}_2\text{O}$ are similarly oriented (Templeton, 1960). The water molecules designated as O(3) are bonded to the rest of the structure by four hydrogen bonds in directions corresponding to a rather distorted tetrahedron.

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